

# Osmotic Coefficients of Aqueous Solutions of Calcium Chloride and Calcium Perchlorate at 25° C

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The osmotic coefficients of solutions of calcium chloride and calcium perchlorate at 25° C have been measured. The binary interaction coefficient ( $\text{Cl}^-$ - $\text{ClO}_4^-$  interaction) is found to have the comparatively high value of  $b_{01} = 0.0444$  mole<sup>-1</sup> kg.

Scatchard's equations (10, 11) for the excess free energy of a mixed electrolyte solution containing two salts of the same charge type can be expressed in the form:

$$\Delta \equiv \nu(\phi - y_A \phi_A^0 - y_B \phi_B^0) = y_A y_B b_{01} I \quad (1)$$

where  $b_{01}$  is a measure of binary ionic interaction. This simplified equation suffices for the system now to be described but the complete equation contains additional terms,  $b_{02}I^2$ ,  $b_{03}I^3$ ... and skew terms such as  $y_A y_B (y_A - y_B)b_{12}I^2$ . An examination of the literature suggests that, for a mixture with a common ion,  $b_{01}$  may be small; for example, it is 0.0038 mole<sup>-1</sup> kg for the NaCl-NaBr system (2), indicating that  $\text{Cl}^-$ - $\text{Br}^-$  interaction is weak; on the contrary, for the NaCl-KCl system (4, 9),  $b_{01} = -0.0253$  mole<sup>-1</sup> kg, corresponding to comparatively strong  $\text{Na}^+$ - $\text{K}^+$  interaction. That the anion-anion interaction is not always weak is demonstrated by the work of Yoest (8, 13) who found  $b_{01} = 0.1225$  mole<sup>-1</sup> kg for the  $\text{CuCl}_2$ - $\text{Cu}(\text{ClO}_4)_2$  system, showing that  $\text{Cl}^-$ - $\text{ClO}_4^-$  interaction, in contrast to that of  $\text{Cl}^-$ - $\text{Br}^-$  is strong. This paper presents measurements on the  $\text{CaCl}_2$ - $\text{Ca}(\text{ClO}_4)_2$  system.

## MATERIALS

A stock solution of calcium chloride was made from calcium carbonate and hydrochloric acid by the method of Stokes (12). A stock solution of calcium perchlorate was prepared from calcium carbonate and perchloric acid by a method already described (6). Portions of these solutions were mixed and diluted for isopiestic vapor pressure measurements.

## METHOD

The application of the isopiestic vapor pressure method to mixed salt solutions was essentially that described in earlier publications (4, 7).

## RESULTS

The experimental data are given in Table I, where  $m_{\text{ref}}$  is the molality of a solution containing calcium chloride only and  $m$  that of a mixed salt solution of the same vapor pressure. Two mixtures were used, in one of which  $y_B$  was 0.3064 and in the other 0.6344. Table I gives the osmotic coefficients of these mixed salt solutions and values of  $\Delta/(y_A y_B I)$ .

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## DISCUSSION

The osmotic coefficients given in the third and sixth columns of Table I are probably reliable to within 0.001; an error of this magnitude corresponds to an uncertainty of 0.003 in  $\Delta$  and of 0.0025 in  $\Delta/(y_A y_B I)$  for the most dilute solution and correspondingly less for the more concentrated solutions.

The average value of  $\Delta/(y_A y_B I)$  is 0.0477 mole<sup>-1</sup> kg at  $y_B = 0.3064$  and 0.0412 mole<sup>-1</sup> kg at  $y_B = 0.6344$ ; this difference is not sufficient to justify the use of the  $(y_A - y_B)$  skew term in Equation 1. Moreover, there seems to be no significant trend in the values of  $\Delta/(y_A y_B I)$  with a change in  $I$  and, therefore, there is no need for additional terms such as  $b_{02}I^2$  in Equation 1. The average of all 26 determinations,  $b_{01} = 0.0444$  mole<sup>-1</sup> kg, is a measure of  $\text{Cl}^-$ - $\text{ClO}_4^-$  interaction in this system. It is much larger than that for  $\text{Cl}^-$ - $\text{Br}^-$  interaction in the NaCl-NaBr system (2) but smaller than that found by Yoest (13) for  $\text{Cl}^-$ - $\text{ClO}_4^-$  interaction in the  $\text{CuCl}_2$ - $\text{Cu}(\text{ClO}_4)_2$  system.

If  $b_{01}$  is a measure of binary interaction between two anions, it should be independent of the cations,  $\text{Ca}^{2+}$  and  $\text{Cu}^{2+}$  in this case. However, for these two systems,  $b_{01}$  has very different values. The reason for this, it is suggested, lies in the peculiar properties of cupric chloride. There is considerable evidence that this salt forms  $\text{CuCl}^+$ , either a contact ion-pair or as the first stage in the formation of higher complexes such as  $\text{CuCl}_2^+$ . Two lines of evidence are now quoted. Figure 1 shows the osmotic coefficients of calcium perchlorate (6), calcium chloride (12), cupric

Table I. Osmotic Coefficients of Aqueous Solutions of Calcium Chloride and Calcium Perchlorate at 25° C

$m_{\text{ref}}$	$m$	$y_B = 0.3064$		$y_B = 0.6344$		
		$\phi$	$\Delta/(I y_A y_B)$	$\phi$	$\Delta/(I y_A y_B)$	
2.017	1.905	1.464	0.0596	1.825	1.528	0.0496
2.202	2.078	1.540	0.0629	1.988	1.610	0.0601
2.483	2.344	1.654	0.0498	2.243	1.729	0.0377
2.795	2.641	1.791	0.0513	2.525	1.873	0.0410
3.210	3.035	1.971	0.0454	2.898	2.065	0.0451
3.656	3.460	2.159	0.0415	3.307	2.259	0.0365
4.118	3.901	2.353	0.0410	3.730	2.461	0.0369
4.771	4.521	2.624	0.0436	4.324	2.744	0.0445
5.321	5.037	2.834	0.0413	4.824	2.959	0.0377
6.074	5.709	3.083	0.0440	5.463	3.222	0.0335
6.795	6.327	3.275	0.0475	6.030	3.436	0.0366
7.385	6.794	3.388	0.0491	6.442	3.573	0.0420
7.970	7.247	3.464	0.0429	6.833	3.674	0.0341

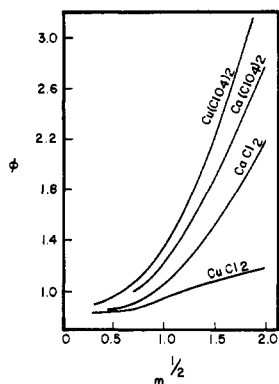


Figure 1. Dependence on concentration of the osmotic coefficients of cupric perchlorate (3), calcium perchlorate (6), calcium chloride (12), and cupric chloride (5)

perchlorate (3), and cupric chloride (5). The curves for the first three salts are typical of fully dissociated, highly solvated electrolytes; that for cupric chloride is such as to suggest incomplete dissociation. Spectrophotometric measurements of cupric chloride in lithium chloride solution (1) suggest that formation of  $\text{CuCl}^+$  is likely. Any such reduction in the number of  $\text{Cu}^{2+}$  ions in a  $\text{CuCl}_2$  solution suffices to explain, at least qualitatively, why  $b_{01}$  is different in the  $\text{CaCl}_2\text{-Ca}(\text{ClO}_4)_2$  and  $\text{CuCl}_2\text{-Cu}(\text{ClO}_4)_2$  systems.

#### NOMENCLATURE

$\phi$  = osmotic coefficient of a mixed salt solution  
 $\phi_A^0, \phi_B^0$  = osmotic coefficients of solutions of salts A and B,

respectively, at ionic strength equal to the total ionic strength of the mixed salt solution,  $I$

$y_A = m_A/m, y_B = m_B/m$   
 $m_A$  and  $m_B$  = molalities ( $\text{mole kg}^{-1}$ ) of A and B, respectively, in the mixed salt solution

$$m = m_A + m_B$$

$$\Delta \equiv \nu(\phi - y_A\phi_A^0 - y_B\phi_B^0)$$

In this paper,  $A = \text{CaCl}_2, B = \text{Ca}(\text{ClO}_4)_2, \nu = 3$

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## Densities of Some Nitrate and Sulfate Melts

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The densities of  $\text{NaNO}_3\text{-KNO}_3$  (45:55 mol %),  $\text{LiNO}_3\text{-KNO}_3$  (41:59),  $\text{KNO}_3\text{-LiNO}_3$  (41:59), and  $\text{NaNO}_3\text{-LiNO}_3$  (46:54) melts are reported for a temperature range of some 200° together with that of  $\text{Li}_2\text{SO}_4\text{-Na}_2\text{SO}_4\text{-K}_2\text{SO}_4$  eutectic at 550° C. Molar volumes of the nitrate mixtures are additive to within 1.3%.

Although the densities of several molten nitrate mixtures are recorded in the literature, the data for four mixtures, employed in a series of electrochemical investigations, are not known. It was therefore necessary to make density measurements of these, and the values have been compared with those calculated upon the assumption of additivity of molar volumes. The density of a ternary sulfate eutectic, also a common solvent, was also measured and is recorded here.

#### EXPERIMENTAL

Densities were measured by the buoyancy method favored for its simplicity coupled with accuracy (3). A silver bob (about 2 cm length), suspended on a 1-mm diameter silver wire below an analytical balance, was immersed to  $10 \pm 1$  mm below the surface of the melt in a glass container.

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The  $\pm 1\text{-mm}$  error represents a volume error of  $\pm 8 \times 10^{-4}$  cc or  $\pm 0.02\%$ . Temperatures were measured by a chromel-alumel thermocouple immersed in the melt and were controlled by a Proportio Null, 1300 Series, controller (Cole-Parmer Instrument and Equipment Co.) connected to the power circuit of a simple box furnace.

In making temperature measurements, the zero point was ice water, and recordings were taken from a Cropico Type P3 potentiometer. The thermocouples were calibrated against the fixed points (mp of ice, Sn, Cd, Pb, and Zn, bp of water) used to define the International Temperature Scale of 1948 (4), a pressure correction being included. In taking measurements, a constancy of  $\pm 0.0005$  gram and  $\pm 0.25^\circ\text{C}$  for 15 min was required, and both heating and cooling cycles were used for each system. The volume of the silver bob as a function of temperature from 325° to 475° C was obtained by measuring the density of sodium nitrate which is given by ref. 6:

$$\rho = 2.125 - 7.15 \times 10^{-4} T \text{ (}^\circ\text{C)}$$